# Modeling the Limits and Effects of Energy Extraction from Tidal Streams

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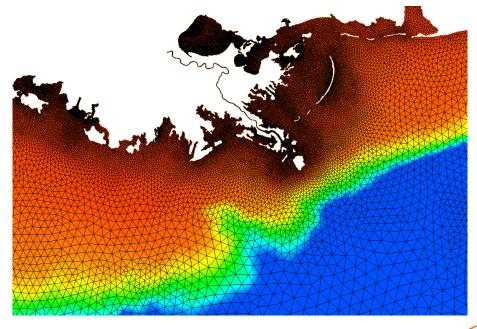
#### Far-field Modeling Support to Accelerate MHK Energy Deployment

- Energy resource assessment
  - Maximum and <u>practical</u> extractable energy
- Environmental impacts
  - Flow fields
  - Flushing time
  - Biogeochemical transport processes
- Efficiency of energy extraction
  - Array optimization and device siting
  - 3-D effects
- Permitting process
  - Clean Water Act



#### Coastal Ocean Model – FVCOM

- 3D Finite Volume Coast Ocean Model (FVCOM)
- Unstructured grid best suited for complex geometry
- MHK module developed by PNNL
- Wetting and drying simulation
- Baroclinic simulation
- Water quality
- Sediment transport
- Coupled wave model
- Public domain
- Parallel computation





### MHK Modeling Approach

- Implementation of MHK energy device in FVCOM using momentum sink approach
- Governing equations with MHK effect

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} - fv = -\frac{1}{\rho_o} \frac{\partial P}{\partial x} + \frac{\partial}{\partial z} \left( K_m \frac{\partial u}{\partial z} \right) + F_u - F_{MHK-u}$$

$$\frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} + w \frac{\partial v}{\partial z} + fu = -\frac{1}{\rho_o} \frac{\partial P}{\partial y} + \frac{\partial}{\partial z} \left( K_m \frac{\partial u}{\partial z} \right) + F_v - F_{MHK-v}$$

- Momentum sinks

Turbine blades 
$$S_1 = -\frac{1}{2}(C_T + C_b)A_b |\vec{u}|^2$$

$$S_2 = -\frac{1}{2} C_p A_p \left| \vec{u} \right|^2$$

$$S_{2} = -\frac{1}{2} C_{p} A_{p} |\vec{u}|^{2}$$

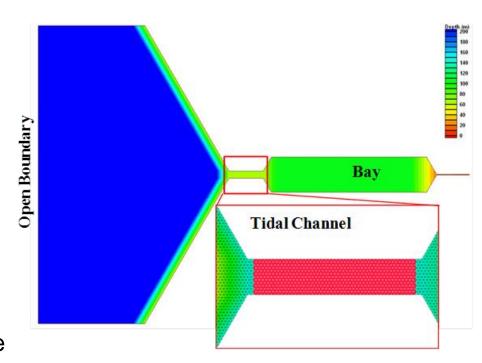
$$S_{3} = -\frac{1}{2} C_{f} A_{f} |\vec{u}|^{2}$$



### **Technical Approach**

#### Validation to analytical solution

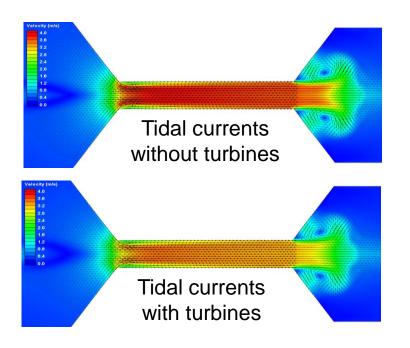
- Idealized tidal channel and bay with realistic dimensions and forcing
- Open boundary M2 tide (2m range)
- User-friendly MHK parameter input
  - Turbine elevation from seabed
  - Turbine diameter
  - Turbine thrust coefficient
  - Turbine blade drag coefficient
  - Areas of supporting poles and base
  - Drag coefficients for poles and base

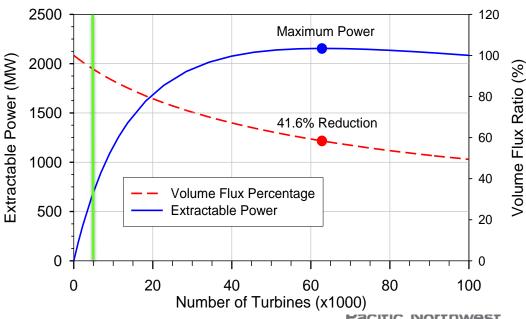


<b>Open Water</b>	Channel Dimension (m)			Basin Dimension (m)			_
Depth (m)	Length	Width	Depth	Length	Width	Depth	
200	30,000	6,000	60	150,000	20,000	100	est

#### MHK Model Validation

- MHK model results agree well with analytical solution by Garrett & Cummins (2004, 2005)
  - Extractable Max Power = Function of (tidal amplitude, volume flux)  $P_{model} = 2,154 \text{ MW}; P_{analytical} = 2,169 \text{ MW}$
  - Diminishing return of extractable power occurs when volume flux reduces by 42%





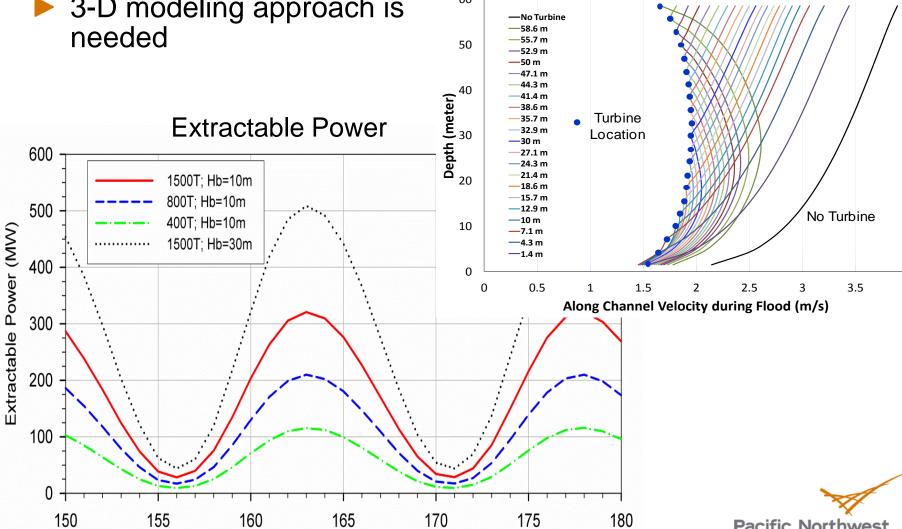
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### Efficiency – Effects of Hub Height & Array Size

Velocity Profiles vs. Turbine Height

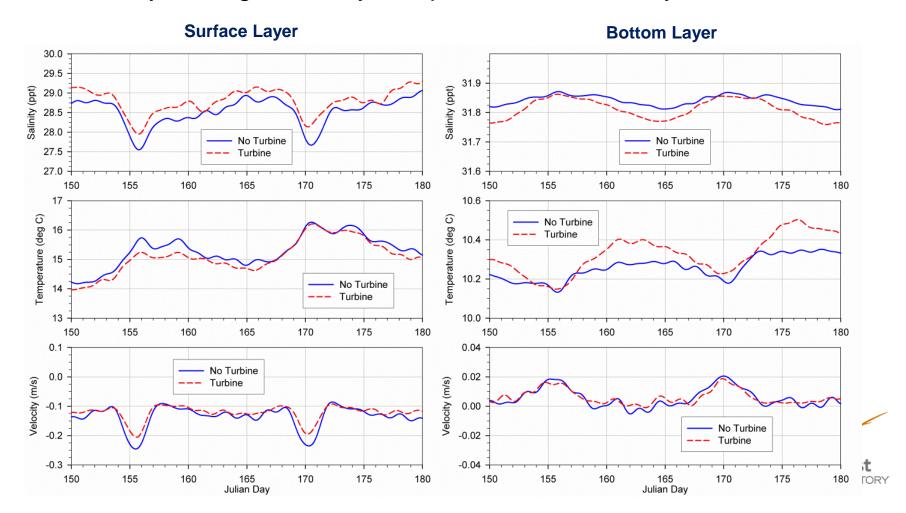
60 3-D modeling approach is -No Turbine --58.6 m

Julian Day



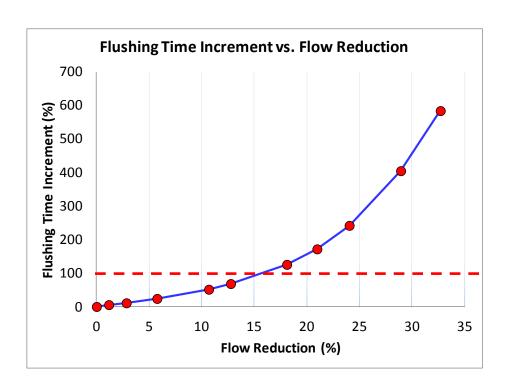
## **Environmental Impacts – Mixing & Circulation**

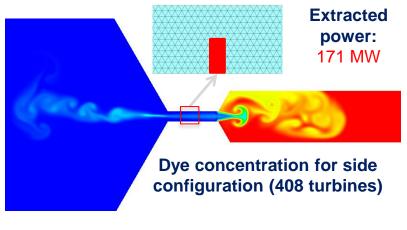
- Year-long simulations of the tidal channel and bay system forced with tide, heat flux and river run-off
  - Tidally-averaged salinity, temperature and velocity in the channel

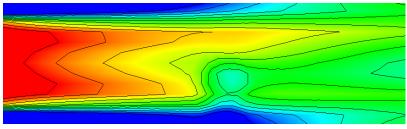


### **Environmental Impacts - Flushing Time**

► Effect on flushing time of a tidal basin – nonlinear effect





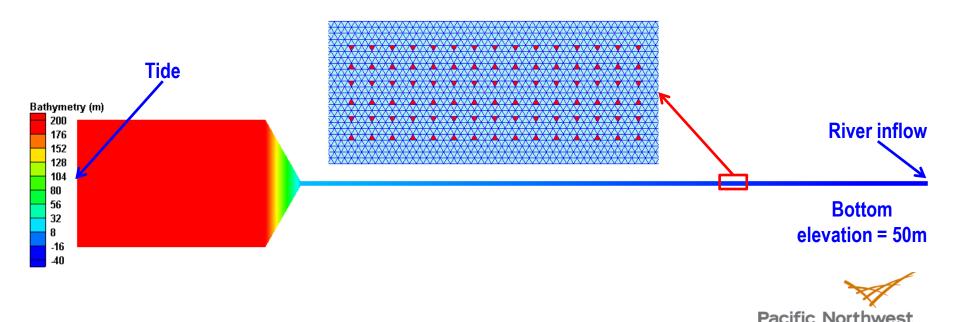


**Velocity for MHK Side Configuration** 



#### **Model Applications - River In-streams**

- Energy extraction in river in-streams
  - Cumulative effect and interaction of multiple projects
  - Change of hydrodynamic conditions at local and system scales
- An idealized river connected to a bay forced with tide
  - Bay depth = 200m; length = 100km; width = 750m; slope =  $5x10^{-4}$
  - 10 projects along the river with 90 turbines per project

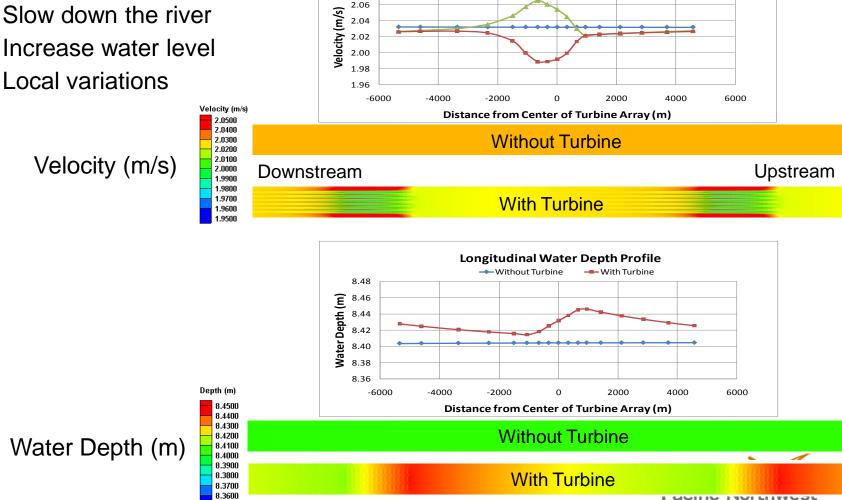


#### Effect of Energy Extraction on River Streams

2.08

- Effects on local and system-wide scales

8.3500



**Longitudinal Velocity Profile** 

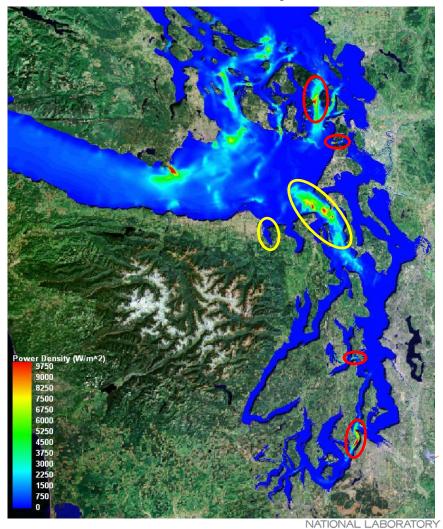
--- Between Turbine Array --- Align with Turbine Array

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# **Accelerate MHK Energy Development –** Identify Hotspots in the Real World

#### **Tidal Current Magnitude**

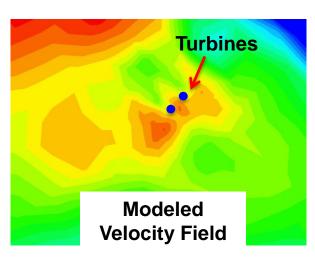
#### **Power Density**

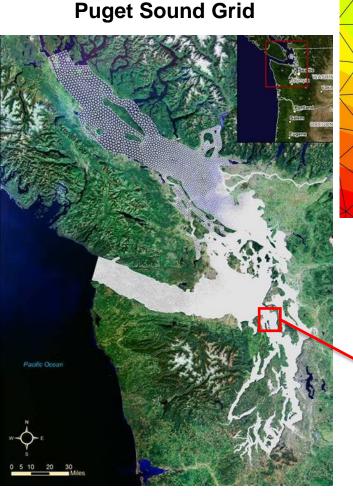


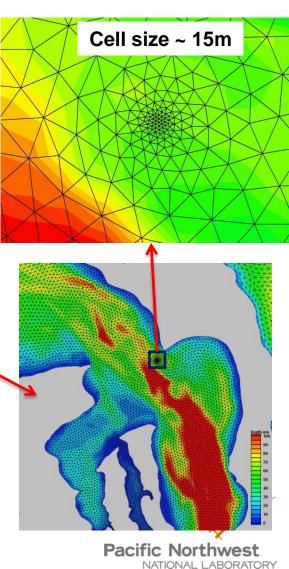
# Snohomish PUD Pilot Study in Admiralty Inlet

#### **Two Open-Hydro Turbines**









# Thank you

